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# A dynamical systems perspective on the absence of debris associated with the disappearance of flight MH370

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**Lagrangian  
descriptors and the  
surface search for  
MH370**

V. J. García-Garrido et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures



Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



## Abstract

The disappearance of Malaysia Airlines flight MH370 on the morning of the 8 March 2014 is one of the great mysteries of our time. Perhaps the most relevant aspect of this mystery is that not a single piece of debris from the aircraft has been found. Difficulties in the search efforts, due to the uncertainty in the plane's final impact point and the time that has passed since the accident, bring the question on how the debris has scattered in an always moving ocean, for which there are multiple data sets that do not uniquely determine its state. Our approach to this problem is based on the use of Lagrangian Descriptors (LD), a novel mathematical tool coming from dynamical systems theory that identifies dynamic barriers and coherent structures governing transport. By combining publicly available information supplied by different ocean data sources with these mathematical techniques, we are able to assess the spatio-temporal state of the ocean in the priority search area at the time of impact and the following weeks. Using this information we propose a revised search strategy by showing why one might not have expected to find debris in some large search areas targeted by the Australian Maritime Safety Authority (AMSA), and determining regions where one might have expected impact debris to be located and that have not been subjected to any exploration.

## 1 Introduction

The fate of Malaysia Airlines flight MH370 has been a mystery since its disappearance on the morning of the 8 March 2014. An analysis of radar data, aircraft performance calculations and satellite communication (SATCOM) system signaling messages placed the aircraft over an arc, the 7th arc, in the southern part of the Indian Ocean (ATSB, 2014a), where the aircraft's fuel was, presumably, exhausted. Refinements to the analysis of both the flight and satellite data have been continuous since the loss of MH370 and have resulted in the definition of several potential impact regions along the 7th arc, driving the search efforts to consider different search areas.

**NPGD**

2, 1197–1225, 2015

## Lagrangian descriptors and the surface search for MH370

V. J. García-Garrido et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures



Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



The events determining the plane's fate after the crash were undoubtedly affected by the manner in which the impact occurred, since this should have determined the nature of the breakup of the plane into pieces of debris. A recent study by Chen et al. (2015) has conjectured that the plane's impact was under conditions in which no debris was produced and therefore no plane pieces could have been found by the search services. The search services, however, accepted that after the plane's disappearance, debris should have been produced and began one of the most challenging searches in aviation history. During several months a surface search was conducted that implicitly assumed the presence of floating debris. It was not until October 2014 that the much more demanding underwater search was started. It is hard to know what should be the properties of the debris produced after the impact, and some aspects in this respect are discussed by Chen et al. (2015). Given the highly speculative status of all the events related to Malaysia Airlines flight MH370, in this work we will assume the presence of fuselage pieces similar to those recovered from the Air France Flight 447 flight, (see <http://www.aviationlawmonitor.com/tags/air-france-flight-447/>) which consisted of thin, flat, half submerged structures, or personal flotation devices, which potentially would have been driven mainly by ocean currents. Under these assumptions – which are consistent with the plan and actions taken by the search services – it is then clear that it is important to understand the nature of the ocean currents in the impact area (Saab, 2014) at the time of disappearance and thereafter, and to then determine how they contributed to debris dispersion. We will assume that it is reasonable to relate the evolution of the described potential debris with that of surface drifters, such as those distributed by the Global Drifters Program (GDP), and for this reason, in order to support our study, we will benchmark our conclusions with these drifters tracks.

Differences between the forecasted velocity fields are a handicap for the analysis of particle dispersion, and therefore having a good representation of the ocean circulation patterns becomes crucial for dispersion studies (Mendoza et al., 2014; Griffa et al., 2013; Haza et al., 2007). Mainly two type of data sources for oceanic currents are available in oceanic contexts. One is obtained in almost real time after post-processing

**Lagrangian  
descriptors and the  
surface search for  
MH370**

V. J. García-Garrido et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures



Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



satellite altimetry, such as AVISO products, which provide mainly geostrophic currents. Similar products integrating surface winds and/or Ekman dynamics are, for instance, OSCAR and SCUD.

Alternatively, surface ocean currents can be provided by physics-based computational models which are solved on high-resolution meshes. These provide ocean circulation currents in space and time on the whole oceanic basin under study and, in order to be representative of the ocean state, they usually assimilate AVISO data and drifters and incorporate other important dynamics and measurements. Examples of these models are the Hybrid Coordinate Ocean Model (HYCOM), or the Operational Mercator global Ocean analysis and forecast system (provided by EU Copernicus). Typically these products provide high resolution space-time data sets but only in areas of interest to the countries funding the consortia providing simulations. In this study the focus is in the middle of the Indian Ocean, where only low resolution data is available.

This study is focused in the analysis of AVISO and HYCOM data predictions for the region and period of interest. Our analysis utilizes fundamental ideas coming from dynamical systems theory applied to Lagrangian transport, which provide sharper insights than the simple drifter tracking supplied by tools such as GNOME or SCUD. The approach taken by the rescue services as described in ATSB (2014a) seems to be closer to a simple drifter tracking approach, and no information is provided on the type of velocity fields used.

Dynamical systems theory contributes to this problem by realizing Poincaré's idea of seeking geometrical structures in the phase portrait (for this problem, the ocean surface) that can be used to organize schematically regions corresponding to qualitatively different types of trajectories. These geometrical objects, the stable and unstable manifolds of hyperbolic trajectories, also called Lagrangian structures, are expected to be robust with respect to slight perturbations of the velocity field. The main contribution from this perspective is the consideration that the analysis of individual trajectories may be misleading, and that the right approach to take is to observe the consistency of in-

## Lagrangian descriptors and the surface search for MH370

V. J. García-Garrido et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures



Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



dividual trajectories with the dynamical barriers highlighted by the Lagrangian skeleton of the velocity field.

Finding these structures in the context of geophysical flows is a dynamical systems challenge, as these velocity fields are time dependent and only known on a finite time data set. Their study requires the use of modern techniques in nonlinear dynamical systems theory that achieve a phase portrait representation for systems with these characteristics. In this context many tools have been successful to this end and have provided interesting insights into oceanic problems. For instance, manifolds have been approximated by computing ridges of fields, such as finite size Lyapunov exponents (FSLE) (Aurell et al., 1997) successfully applied into oceanic contexts (d'Ovidio et al., 2004; Kai et al., 2009) and finite time Lyapunov exponents (FTLE) (Nese, 1989; Shadden et al., 2005, 2009). Another perspective within the geometrical approach different from Lyapunov exponents is that provided by distinguished hyperbolic trajectories (DHT), a generalization of the concept of fixed point for dynamical systems with a general time dependence (Ide et al., 2002; Ju et al., 2003; Madrid and Mancho, 2009), and their stable and unstable manifolds (Mancho et al., 2006c; Mendoza and Mancho, 2012). In this approach stable and unstable manifolds are directly computed as material surfaces (Mancho et al., 2003, 2004). This method has also provided valuable insight into oceanic problems (Mancho et al., 2006a; Mendoza et al., 2010). Other approaches in this field have been the geodesic theory of Lagrangian Coherent Structures (LCS) (Haller and Beron-Vera, 2012), the variational theory of LCS (Farazmand and Haller, 2012), the trajectory complexity measures (Rypina et al., 2011), mesohyperbolicity measures and ergodic partitions (Mezic and Wiggins, 1999; Mezic et al., 2010) and transfer operator methods (Froyland et al., 2012; Froyland and Padberg-Gehle, 2014).

A recent tool that reveals phase space structures of general time dependent dynamical systems is the so-called function  $M$ , also referred to as Lagrangian Descriptors (see for instance Mendoza and Mancho, 2010, 2012; Mancho et al., 2013), for which several advantages have been discussed in Mancho et al. (2013), Rempel et al. (2013)

## Lagrangian descriptors and the surface search for MH370

V. J. García-Garrido et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



and de la Cámara et al. (2012, 2013) vs. other classical approaches (Shadden et al., 2005; Mezic and Wiggins, 1999). We illustrate the power of this proposed methodology jointly with techniques based on contour advection (Dritschel, 1989; Mancho et al., 2003) to reach conclusions regarding the fate of the plane debris in the weeks after the accident.

In this paper we analyze the transport processes arising from AVISO and HYCOM velocity fields. In order to assess the performance (quality) of the ocean state data for the time period and region under consideration we compute for each data set the Lagrangian geometrical skeleton by means of the function  $M$ , which is then benchmarked with GDP surface drifter tracks. We find that drifters remarkably follow the Lagrangian skeleton provided by AVISO data. HYCOM data presents high-frequency motions, but still our Lagrangian techniques highlight mesoscale structures analogous to those found in AVISO. By combining contour advection of the presumed impact areas and the geometrical skeleton of the underlying flow we note the presence of ocean mesoscale structures, which could have acted as barriers for the debris. Additionally it is observed that the impact area evolves in such a way that it fills quiet ocean regions, suggesting that they are a very likely destination for the debris. Interestingly, our Lagrangian analysis reaches conclusions that could have guided the search tasks: it highlights regions disregarded by the search efforts, where debris could have been found, and points out that debris could scarcely have visited certain regions subjected to intense search.

The structure of this article is as follows. Section 2 describes the data used in this study. Section 3 describes and discusses the approach to the debris dispersion. Section 4 provides the results and the discussion. Finally, Sect. 5 provides the conclusions.

## 2 Data

The first data source of velocity fields used for this work has been obtained from satellite altimetry produced by Ssalto/Duacs and distributed by AVISO, with support from

### Lagrangian descriptors and the surface search for MH370

V. J. García-Garrido et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures



Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



CNES, and are downloadable from <http://www.aviso.oceanobs.com/duacs/>. In particular we have considered the product UPD, which is reconstructed from four satellites. The data are given on a spatial grid of  $1080 \times 915$  points (longitude/latitude). The latitude ranges from  $82^\circ$  S to  $81.9746^\circ$  N using a Mercator projection, and the longitude ranges from 0 to  $359.667^\circ$  using a uniform grid. The spatial precision is thus  $1/3^\circ$  at the Equator and is provided with daily frequency. AVISO data essentially reproduces geostrophic currents. A priori, the convenience of using this type data for our study is supported by work discussed in Olascoaga et al. (2013) and Mendoza et al. (2014), and eventually is confirmed by the results reported in the discussion section.

A second source used for the velocity fields is the Hybrid Coordinate Ocean Model (HYCOM) (Bleck, 2002; Chassignet et al., 2007), which provides velocity fields throughout the entire ocean depth. This model assimilates satellite sea-surface height and temperature data by means of the Navy Coupled Ocean Data Assimilation (NCODA) system and it is forced by surface winds and air-sea fluxes. In particular, we have considered the GLBa0.08 data set (experiments expt\_91.0 and expt\_91.1), which can be downloaded from <http://hycom.org/dataserver/glb-analysis/>. These experiments use 32 layers along the vertical coordinate and are carried out over a global Mercator curvilinear grid for the ocean, where latitude ranges from  $78^\circ$  S to  $47^\circ$  N and the equatorial resolution is  $1/12^\circ$ , resulting in a grid point spacing of approximately 7 km on average. Regions north of  $47^\circ$  N are represented with a bipolar patch. The data is provided daily.

HYCOM data incorporates several physical factors that introduce high-frequency variability, and produce velocity fields that, at least in the very upper layers, are far from geostrophy. In the next section we will discuss issues of finite resolution and noise effects in relation to the debris dispersion problem. In the calculations performed we attempt to filter the high-frequency variability by using the HYCOM data layer at 50 m depth. A similar depth choice for this model is used, for instance, in Sulman et al. (2013) or for CUPOM (Colorado University Princeton Ocean Model) in Branicki and Kirwan (2010). In the latter work the authors show how the resulting Lagrangian struc-

## Lagrangian descriptors and the surface search for MH370

V. J. García-Garrido et al.

[Title Page](#)[Abstract](#)[Introduction](#)[Conclusions](#)[References](#)[Tables](#)[Figures](#)[Back](#)[Close](#)[Full Screen / Esc](#)[Printer-friendly Version](#)[Interactive Discussion](#)



ture is close to 2-D surfaces that extend nearly vertically into the water column. The full 3-D Lagrangian structures can be obtained by a vertical extension of the evolving stable and unstable manifolds calculated in the 2-D plane, but this is valid only throughout a layer whose thickness depends on the ratio of the characteristic velocity within the 2-D slice to the characteristic vertical shear of the horizontal velocities (Branicki and Kirwan, 2010; Branicki et al., 2011). We confirm that this is the case in our study.

Finally, in order to benchmark the Lagrangian structures calculated for the velocity field data sets described above, surface drifter tracks are obtained from data distributed by the Global Drifters Program (GDP), from the National Oceanic and Atmospheric Administration (NOAA) and Atlantic Oceanographic and Meteorological Laboratory (AOML). These tracks can be downloaded from <http://www.aoml.noaa.gov/phod/dac/index.php>. Each drifter has an identification number with five digits, which allows for the identification of different drifters. The sampling of the drifter position is once every 6 h.

### 3 Modelling debris dispersion

The debris produced after a plane's accident is due to the breakup of the plane and it depends on how it enters the water. Large heavy and unbroken pieces of fuselage would sink rapidly. However, there exist reports of plane accidents (Chen et al., 2015) which produced debris spread over a wide area, with light pieces that might have floated for a long time. This article, as described in the Introduction, is focused on the search for this type of debris, such as flat wide objects not surpassing the waterline, and thus not subjected to wind sailing effects, that would have been mainly driven by ocean currents. We will assume a similarity between this debris and drifter motion.

Kuznetsov et al. (2002) have examined the role played by Lagrangian structures obtained in the Gulf of Mexico. In particular, they have analyzed data from the Colorado University Princeton Ocean Model and have compared the geometry of the dynamics with simultaneous trajectories of drifters measured in an independent way. Indirectly,

## Lagrangian descriptors and the surface search for MH370

V. J. García-Garrido et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion





the agreement between drifter evolution and the Lagrangian patterns of purely advected particles has served as a confirmation of the model quality. Also, Beron-Vera et al. (2010) compares the quality of two different altimetry AVISO products based on the agreement between a drifter trajectory and the Lagrangian skeleton supplied by the FTLE.

Recent studies (Tallapragada and Ross, 2008; Beron-Vera et al., 2015) have considered deviations in the evolution of drifters from that of purely advected particles by taking into account inertial effects produced by the buoyancy of the object and their finite size. Their approach considers the Maxey–Riley equation (Maxey and Riley, 1983) which holds for small rigid spheres. Considering the diversity of potential shapes for the debris objects, and that mainly we are considering flat, wide objects, quite different from a sphere, we do not consider this approach in our study. We disregard this choice because it is at least as speculative as the straightforward Lagrangian approach for purely advected particles, and for this reason the latter is the one we take. In the end, the agreement found between the GDP drifters tracks and the mesoscale features that our tools highlight supports this decision. In this way we consider the motion of the airplane debris as that of purely advected particles. Such particles follow trajectories  $x(t)$  in the ocean that evolve according to the dynamical system:

$$\frac{dx}{dt} = v(x(t), t) \quad (1)$$

where  $v(x(t), t)$  is the velocity field of the ocean region of interest. In our analysis, as previously explained, we will assume that the motion of particles is mainly horizontal. The equations of motion that describe the horizontal evolution of particle trajectories on a sphere of radius  $R$  are:

$$\frac{d\lambda}{dt} = \frac{u(\lambda, \phi, t)}{R \cos \phi}, \quad (2)$$

$$\frac{d\phi}{dt} = \frac{v(\lambda, \phi, t)}{R}. \quad (3)$$

## Lagrangian descriptors and the surface search for MH370

V. J. García-Garrido et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



Here the variables  $(\lambda, \phi)$  are longitude and latitude,  $u$  and  $v$  respectively represent the eastward and northward components of the velocity field provided by the data set.

For our Lagrangian analysis, which is based on Lagrangian Descriptors (function  $M$ ) and also on contour evolution, it is necessary to integrate Eqs. (2) and (3) in order to compute particle trajectories. As the velocity field for the system (Eqs. 2 and 3) is provided solely on a discrete space-time grid, the first issue to deal with is that of interpolation. We have used bicubic interpolation in space and third order Lagrange polynomials in time according to the details given in Mancho et al. (2006b) and Mendoza et al. (2014). This assumes smoothness of the velocity field below the resolution which, on the other hand, is rather low.

An open question here is how robust are Lagrangian techniques when dealing with ocean motions that do not vary smoothly at small scales, as those having an inherent turbulent nature. Recent work by Hernández-Carrasco et al. (2011) analyze this question by looking at the impact on FTLE of the two major effects when dealing with real data, namely, noise and dynamics of unresolved scales. Their work concludes that, although some features are lost, this tool still gives an accurate picture of the oceanic transport properties. We take these conclusions as supportive of our assumptions in the interpolation scheme that we use. On the other hand, effects of high frequency variations on the velocity field are also included in the HYCOM data. In the last section we will highlight common features between this and the more smooth AVISO data, which will support also the conclusions in Hernández-Carrasco et al. (2011).

## 4 Results and discussion

### 4.1 The Lagrangian skeleton

The global nature of particle trajectories generated by Eq. (1) can be understood through the spatio-temporal template formed by geometrical structures of the flow that organize trajectories into distinct ocean regions, corresponding to qualitatively differ-

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



ent types of trajectories. The boundaries or barriers between these regions are time dependent material surfaces (which, mathematically, are invariant manifolds). Such a spatio-temporal template can be constructed with the technique that is referred to as Lagrangian Descriptors (LD), based on a function, function  $M$  (see Madrid and Mancho, 2009; Mendoza and Mancho, 2010; Mancho et al., 2013), defined as follows:

$$M(\mathbf{x}_0, t_0) = \int_{t_0-\tau}^{t_0+\tau} \|\mathbf{v}(\mathbf{x}(t), t)\| dt. \quad (4)$$

Here  $\|\cdot\|$  stands for the modulus of the velocity vector. At a given time  $t_0$ , function  $M(\mathbf{x}_0, t_0)$  measures the arclength traced by the trajectory starting at  $\mathbf{x}_0 = \mathbf{x}(t_0)$  as it evolves forwards and backwards in time for a time period  $\tau$ . The structure of the function  $M$  shows, at low  $\tau$  values, a smooth pattern such as that visible in Fig. 1a. There,  $M$  has been evaluated for AVISO data, on the date of the plane crash and near one of the search areas, using an integration period of  $\tau = 5$  days. On the other hand, Fig. 1b (computed for  $\tau = 20$  days) illustrates how the structure of  $M$  evolves for large  $\tau$  towards less regular structures. By this we mean that sharp changes of  $M$  values occur in narrow gaps, forming filaments that highlight stable and unstable manifolds. A thorough explanation of this effect is discussed in (Mendoza and Mancho, 2010, 2012), Mancho et al. (2013) and Lopesino et al. (2015). Figure 1c shows a different projection for the latter case, which highlights the singular features of  $M$  aligned with stable and unstable invariant manifolds, and their crossing in a hyperbolic point. We remark that the information contained in these figures is obtained by means of integration of particle trajectories. In fact some of the figures reported in this article use tens of thousands of them. The difference in this analysis with respect to that performed by the drifter tracking approach taken by ATSB (2014a, b), or other tools such as GNOME or SCUD, is the way in which this information is displayed. The latter tend to represent this output as spaghetti diagrams, while our Lagrangian perspective finds geometrical structures

## Lagrangian descriptors and the surface search for MH370

V. J. García-Garrido et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures



Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



on the ocean surface, that are used to distinguish regions corresponding to qualitatively different types of trajectories.

Large  $M$  values, represented in reddish colors, are related to regions of high speed fluid (such as jets), while bluish colors denote calm regions. Figure 1d schematically shows the manifold skeleton and how particles, such as drifters or plane debris would evolve in the neighborhood of this structure. Invariant manifolds are dynamic barriers that cannot be crossed by purely advected particles and control transport in the region. The cross point of the stable and unstable manifolds, the hyperbolic point, drastically bends the trajectories. Tracer blobs evolve constrained by the manifold structure. Figure 1e illustrates this point by showing elongation of blob contours along the unstable manifold of a hyperbolic trajectory and squeezing along its stable manifold. It is important to remark here that, from the dynamical system perspective, the main distortion agents for the contours are those causing their filamentous shape and, as explained here, these agents are the hyperbolic trajectories and their stable and unstable manifolds. Additionally, in the flow there exists regions dominated by trajectories with elliptic type stability, in which, contrary to what happens near hyperbolic trajectories, blobs remain coherent instead of forming filaments. This is illustrated in Fig. 1f. Oceanic eddies are an example of regions displaying such a behaviour (see, e.g. Chelton et al., 2011) and this is also the case for oceanic jets, in which blobs are transported at a high speed but not distorted into filaments (see e.g. Wiggins and Mancho, 2014). Therefore, the interplay between stretching and confinement is an essential ingredient of fluid transport processes.

In this work, the importance of how water masses evolve is clear because of the uncertainty in the plane's impact point, and thus, in order to reach conclusions on the fate of the plane debris, it is important to track the time evolution of areas in which the plane potentially could have crashed, and recognize the constraints on these regions found in the ocean during the period after the accident. The evolution of these areas is tracked with the contour advection algorithm developed by Dritschel (1989), but including some modifications explained in Mancho et al. (2003, 2004, 2006c).

## Lagrangian descriptors and the surface search for MH370

V. J. García-Garrido et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures



Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



## 4.2 Analysis of the MH370 plane debris dispersion

The goal of this section is to analyze the search strategy followed by the Australian Maritime Safety Authority (AMSA), in order to see if, in the light of the tools and data described in the previous sections, alternative search strategies could have been suggested.

One of the major challenges in the first stages of the search was to know how debris had scattered in an always moving ocean. On Tuesday 18 March and on Wednesday 19 March search areas were defined by AMSA according to possible flight paths deduced from satellite and aircraft performance data which assumed impact points along the 7th arc. The charts released by AMSA for the different surface search areas are available at <http://www.amsa.gov.au/media/incidents/mh370-search.asp>. Figure 2a shows the potential flight paths in white, and the 7th arc in black. The presumable impact area along the 7th arc is depicted in pink. Its width, which is at around 93 km, expresses uncertainties in the impact point. Our discussion is based on this uncertainty band, which was considered as the maximum priority in the reports by ATSB (2014a, b). However, we note that the satellite analysis also has highlighted a wider search band around this narrower strip.

The search area released by AMSA during these days appears in the figure surrounded by a dashed line. Moreover, the gray shaded contour shown in this figure represents the advection of the presumed initial impact area until the 19 March, according to ocean velocity data distributed by AVISO. This analysis thus suggests a smaller search area than the one determined by AMSA for the search operations that took place during the 18 and 19 March. However, one remaining question that needs to be addressed in order to support this conclusion is, how accurate are AVISO data when representing the true ocean state? We provide some discussion of this point in terms of the tools described in the previous subsection. We observe that the advected contour stretches along unstable manifolds, which act as the main deforming agents for this blob. Stable and unstable manifolds and eddies are recognized in the background of

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures



Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



Fig. 2a by means of the function  $M$ . The dark blue regions represent calm ocean regions and their presence is consistent with drifter motions. For instance, drifter 16545, represented by a magenta dot on the 19 March, appears to be in one of these calm regions, and consistently it barely moves. Video S1 confirms that this is the case from the 8 to the 20 March. Similarly, the movie confirms that the drifter 16539 placed in a zone further east, during the period running from the 20 March to the 27 March remains in a blue calm region, scarcely moving, consistent with AVISO data. The agreement between AVISO data and drifter motions supports the adequacy of AVISO to accurately describe the ocean motion.

Satellite imagery provided to AMSA on the 20 March revealed objects that could have been possible debris of the missing Malaysia Airlines flight MH370. Subsequently, the search area was shifted 185 km to the south east of the original search area and the search efforts were focussed in this area from the 20 to the 27 March. This new search area is shown in Fig. 2b limited by a dashed line. The drifter 16539 is now the closest to the new search area. The gray shaded contour represents the advection of the presumed initial impact area along the 7th arc until the 27 March 2014, and the coloring at the background highlights for this day, by means of the  $M$  function, the Lagrangian skeleton. The figure suggests that according to AVISO the debris of a plane that crashed along the 7th arc could not have flowed to this region in this period of time, and thus the objects detected in this area should have had a different origin.

Figure 3a and b proceeds with a similar analysis to that of Fig. 2a and b, but using HYCOM data instead. In the HYCOM simulations, layers near the surface are strongly dominated by wind forcing and, as a result, the velocity fields are subjected to high frequency variations. As explained in Sects. 1 and 2, our study assumes a similarity between debris motion and that of drifters. Mancho et al. (2006a), Branicki and Kirwan (2010) and Sulman et al. (2013) justify the study of Lagrangian structures from velocity fields by considering layers just below the very upper layers which are slightly wind filtered. In Fig. 3a and b the background coloring shows 2-D Lagrangian structures obtained at 50 m depth. The Lagrangian structures now are much more blurred than

# Lagrangian descriptors and the surface search for MH370

V. J. García-Garrido et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures



Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



those obtained from AVISO, but still a comparison is feasible in terms of the mesoscale structures highlighted by the  $M$  function. HYCOM shows mesoscale features linked to the circumpolar current further spread into the north, and the calm region close to drifter 16545 still seems to be present, but rather diffuse and displaced south of the drifter. Figure 3a illustrates that the spreading of the presumed impact area is broader than that computed from AVISO data, but still smaller than the AMSA search area. Further details are found in movie S2. The calm area in which drifter 16539 seemed to be anchored, according to Fig. 3b, now appears as a more active region with diffuse structures. However the HYCOM analysis likewise confirms that the debris of a plane crashing along the 7th arc could have barely reached this region in this period of time.

On the 28 March further refinements of the flight path shifted the search area up to the north, and the newly determined most likely impact area was then the one depicted in Fig. 4a ATSB (2014a) in the northeast direction above the Broken Ridge along the 7th arc. From the 28 March until the 3 April the search services were focused on the area surrounded by the dashed line in Fig. 4a. The background coloring of this figure shows the Lagrangian structures obtained from the  $M$  function evaluated from AVISO data on the 3 April 2014. The presumed initial impact area is advected until this day and represented in the gray shaded region. Its filamented structures clearly tend to be aligned along the unstable manifolds visible in the singular features of  $M$ . Numerous drifters are represented with magenta dots and they move consistently with the highlighted Lagrangian skeleton. This is further confirmed in the video S3. For instance drifter 56566, which, on the day of the accident, is within a strong mesoscale structure, an oceanic eddy placed at the east of the presumed impact area, remains within the eddy during several months, being transported with it towards the west. Similarly, drifters 56947 and 56512 are trapped at some point in weaker eddies. Drifters 56557 and 56502, navigate along stable or unstable manifolds during noticeable periods. The latter drifter, which was placed very close to the presumed search area on the impact day, remains close to the contour after this time interval.

# **Lagrangian descriptors and the surface search for MH370**

V. J. García-Garrido et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures



Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion







into the search panel at the right, but just at the south of the strong jet. We see that the jet acts as a barrier which prevents most of the material of the likely impact area from being transported towards the north, this had the effect of paradoxically concentrating the main search in an area where, according to our analysis, there was likely no debris.

Figure 5a and b shows a similar analysis to that of Fig. 4a and b using HYCOM data at 50 m depth. Mesoscale structures in this data are consistent with those of AVISO. For instance, the large eddy which isolates drifter 56566 is present in a similar position, invading the search area from the 28 March to the 3 April, confirming again that this part could have been excluded from the search. The jet structure splitting the impact region in two is also present at the same position, although somewhat perturbed by wind effects. Similarly to AVISO, much of the material contained in the impact area would evolve filling calm regions which, roughly speaking, are positioned the same. The analysis of Fig. 5b is similar to that of Fig. 4b, and it says that, according to our diagnosis, on the 15 April most of the material in the impact area is outside the search area. Video S4 completes these conclusions.

By the 8 October 2014 the Australia Transport Safety Bureau ATSB (2014b) released a flight path analysis update which indicated that the next underwater phase of the search should be prioritized further south along the 7th arc, and thus a detailed bathymetry was required, and efforts were initiated to obtain this for the zone depicted in Fig. 6. A Lagrangian analysis of the horizontal motions at 2000 m depth confirms that at these depths, the currents are more calm than in upper layers, and consequently the evolution of the impact contour does not spread so much at depth in the ocean. On the other hand, this phase of the search is intended for heavier objects, whose motion would be more gravity dominated than current dominated, and thus horizontal dispersion should not be large for these objects. Movie S5 and Fig. 6 confirm that the north and south bounds of the underwater impact area are the regions in which dispersion is the largest.

## Lagrangian descriptors and the surface search for MH370

V. J. García-Garrido et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



## 5 Conclusions

This work addresses, from the dynamical systems perspective, the fate of the MH370 plane debris after its presumed crash on the morning of the 8 March 2014. This point of view provides a powerful tool for dealing with the difficulty arising from the uncertainty of predictions, which comes from the fact that there are several data sets that define multiple ocean states. The findings described in this paper highlight several facts that could have been relevant to the search for debris associated with MH370. First, we have shown that, according to several available data sources, impact debris from the MH370 plane would have been mainly scattered into calm ocean regions since the material from the likely impact areas tends to fill these areas. Second, mesoscale structures such as ocean eddies and jets may have played a key role in determining forbidden regions and barriers for debris. The consistency found between data obtained from different and independent sources (AVISO, HYCOM, drifters) back the evidence that the mesoscale structures we have described were present in the Indian Ocean during the accident time frame, and that considering these structures could have guided an efficient search procedure. These facts also back the reliability of our dispersion analysis, which would have suggested channeling efforts to regions disregarded from scheduled search areas and bypassing certain regions that were subjected to intense search.

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**NPGD**

2, 1197–1225, 2015

### Lagrangian descriptors and the surface search for MH370

V. J. García-Garrido et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



## References

- ATSB: Australian Transport Safety Bureau: MH370 – Definition of Underwater Search Areas, available at: [http://www.atsb.gov.au/media/5243942/ae-2014-054\\_mh370\\_-\\_definition\\_of\\_underwater\\_search\\_areas\\_18aug2014.pdf](http://www.atsb.gov.au/media/5243942/ae-2014-054_mh370_-_definition_of_underwater_search_areas_18aug2014.pdf) (last access: 20 April 2015), 2014a. 1198, 1200, 1207, 1209, 1211
- ATSB: Australian Transport Safety Bureau: MH370 – Flight Path Analysis Update, available at: [http://www.atsb.gov.au/media/5163181/AE-2014-054\\_MH370%20-FlightPathAnalysisUpdate.pdf](http://www.atsb.gov.au/media/5163181/AE-2014-054_MH370%20-FlightPathAnalysisUpdate.pdf) (last access: 20 April 2015), 2014b. 1207, 1209, 1213
- Aurell, E., Boffeta, G., Crisanti, A., Paladin, G., and Vulpiani, A.: Predictability in the large: an extension of the concept of Lyapunov exponent, *J. Phys. A*, 30, 1–26, 1997. 1201
- Beron-Vera, F. J., Olascoaga, M. J., and Goni, G. J.: Surface ocean mixing inferred from different multisatellite altimetry measurements, *J. Phys. Oceanogr.*, 40, 2466–2480, 2010. 1205
- Beron-Vera, F. J., Olascoaga, M. J., Haller, G., Farazmand, M., Trinanes, J., and Wang, Y.: Dissipative inertial transport patterns near coherent Lagrangian eddies in the ocean, available at: <http://arxiv.org/abs/1408.6512>, last access: 20 April 2015. 1205
- Bleck, R.: An oceanic general circulation model framed in hybrid isopycnic-Cartesian coordinates, *Ocean Model.*, 4, 55–88, 2002. 1203
- Branicki, M. and Kirwan, A. D.: Stirring: the Eckart paradigm revisited, *Int. J. Eng. Sci.*, 48, 1027–1042, 2010. 1203, 1204, 1210
- Branicki, M., Mancho, A. M., and Wiggins, S.: A Lagrangian description of transport associated with a Front-Eddy interaction: application to data from the North-Western Mediterranean Sea, *Physica D*, 240, 282–304, 2011. 1204
- Chassignet, E. P., Hurlburt, H. E., Smedstad, O. M., Halliwell, G. R., Hogan, P. J., Wallcraft, A. J., Baraille, R., and Bleck, R.: The HYCOM (HYbrid Coordinate Ocean Model) data assimilative system, *J. Marine Syst.*, 65, 60–83, doi:10.1016/j.jmarsys.2005.09.016, 2007. 1203
- Chelton, D. B., Schallx, M. G., and Samelson, R. M.: Global observations of nonlinear mesoscale eddies, *Prog. Oceanogr.*, 91, 167–216, doi:10.1016/j.pocean.2011.01.002, 2011. 1208
- Chen, G., Gu, C., Morris, P. J., Paterson, E. G., Sergeev, A., Wang, Y.-C., and Wierzbicki, T.: Malaysia Airlines Flight MH370: water entry of an Airliner, *Not. Am Math. Soc.*, 62, 330–344, 2015. 1199, 1204

## Lagrangian descriptors and the surface search for MH370

V. J. García-Garrido et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures



Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



# Lagrangian descriptors and the surface search for MH370

V. J. García-Garrido et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



de la Cámara, A., Mancho, A. M., Ide, K., Serrano, E., and Mechoso, C.: Routes of transport across the Antarctic polar vortex in the southern spring, *J. Atmos. Sci.*, 69, 753–767, 2012. 1202

de la Cámara, A., Mechoso, R., Mancho, A. M., Serrano, E., and Ide, K.: Quasi-horizontal transport within the Antarctic polar night vortex: Rossby wave breaking evidence and Lagrangian structures, *J. Atmos. Sci.*, 70, 2982–3001, 2013. 1202

d'Ovidio, F., Fernández, V., Hernández-García, E., and López, C.: Mixing structures in the Mediterranean sea from finite-size Lyapunov exponents, *Geophys. Res. Lett.*, 31, L12203, doi:10.1029/2004GL020328, 2004. 1201

Dritschel, D. G.: Contour dynamics and contour surgery: numerical algorithms for extended, high-resolution modelling of vortex dynamics in two-dimensional, inviscid, incompressible flows, *Comput. Phys. Rep.*, 10, 77–146, 1989. 1202, 1208

Farazmand, M. and Haller, G.: Computing Lagrangian coherent structures from variational LCS theory, *Chaos*, 22, 013128, doi:10.1063/1.3690153, 2012. 1201

Froyland, G. and Padberg-Gehle, K.: Almost-invariant and finite-time coherent sets: directionality, duration, and diffusion, ergodic theory, open dynamics, and coherent structures, *Proc. Math. Stat.*, 70, 171–216, 2014. 1201

Froyland, G., Horenkamp, C., Rossi, V., Santitissadeekorn, N., and Gupta, A. S.: Three dimensional characterization and tracking of an Agulhas Ring, *Ocean Model.*, 52–53, 69–75, 2012. 1201

Griffa, A., Haza, A., Özgökmen, T. M., Molcard, A., Taillandier, V., Schroeder, K., Chang, Y., and Poulain, P. M.: Investigating transport pathways in the ocean, *Deep-Sea Res. Pt. II*, 85, 81–95, 2013. 1199

Haller, G. and Beron-Vera, F. J.: Geodesic theory of transport barriers in two-dimensional flows, *Physica D*, 241, 1680–1702, 2012. 1201

Haza, A. C., Griffa, A., Martin, P., Molcard, A., Özgökmen, T. M., Poje, A., Barbanti, R., Book, J., Poulain, P., Rixen, M., and Zanasca, P.: Model-based directed drifter launches in the Adriatic Sea: results from the DART experiment, *Geophys. Res. Lett.*, 34, L10605, doi:10.1029/2007GL029634, 2007. 1199

Hernández-Carrasco, I., López, C., Hernández-García, E., and Turiel, A.: How reliable are finite-size Lyapunov exponents for the assessment of ocean dynamics?, *Ocean Model.*, 36, 208–218, 2011. 1206

## Lagrangian descriptors and the surface search for MH370

V. J. García-Garrido et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



Ide, K., Small, D., and Wiggins, S.: Distinguished hyperbolic trajectories in time-dependent fluid flows: analytical and computational approach for velocity fields defined as data sets, *Nonlin. Processes Geophys.*, 9, 237–263, doi:10.5194/npg-9-237-2002, 2002. 1201

Ju, N., Small, D., and Wiggins, S.: Existence and computation of hyperbolic trajectories of aperiodically time-dependent vector fields and their approximations, *Int. J. Bifurcat. Chaos*, 13, 1449–1457, 2003. 1201

Kai, E. T., Rossi, V., Sudre, J., Weimerskirch, H., Lopez, C., Hernandez-Garcia, E., Marsac, F., and Garçon, V.: Top marine predators track Lagrangian coherent structures, *P. Natl. Acad. Sci. USA*, 106, 8245–8250, 2009. 1201

Kuznetsov, L., Toner, M., Kirwan Jr, A. D., Jones, C. K. R. T., Kantha, L. H., and Choi, J.: The Loop Current and adjacent rings delineated by Lagrangian analysis of the near-surface flow, *J. Mar. Res.*, 60, 405–429, 2002. 1204

Lopesino, C., Balibrea, F., Wiggins, S., and Mancho, A. M.: Lagrangian descriptors for two dimensional, area preserving autonomous and nonautonomous maps, *Commun. Nonlinear Sci.*, 27, 40–51, 2015. 1207

Madrid, J. A. J. and Mancho, A. M.: Distinguished trajectories in time dependent vector fields, *Chaos*, 19, 013111, doi:10.1063/1.3056050, 2009. 1201, 1207

Mancho, A. M., Small, D., Wiggins, S., and Ide, K.: Computation of stable and unstable manifolds of hyperbolic trajectories in two-dimensional, aperiodically time-dependent vector fields, *Physica D*, 182, 188–222, 2003. 1201, 1202, 1208

Mancho, A. M., Small, D., and Wiggins, S.: Computation of hyperbolic trajectories and their stable and unstable manifolds for oceanographic flows represented as data sets, *Nonlin. Processes Geophys.*, 11, 17–33, doi:10.5194/npg-11-17-2004, 2004. 1201, 1208

Mancho, A. M., Hernández-García, E., Small, D., Wiggins, S., and Fernández, V.: Lagrangian transport through an ocean front in the North-Western Mediterranean Sea, *J. Phys. Oceanogr.*, 38, 1222–1237, 2006a. 1201, 1210

Mancho, A. M., Small, D., and Wiggins, S.: A comparison of methods for interpolating chaotic flows from discrete velocity data, *Comput. Fluids*, 35, 416–428, 2006b. 1206

Mancho, A. M., Small, D., and Wiggins, S.: A tutorial on dynamical systems concepts applied to Lagrangian transport in oceanic flows defined as finite time data sets: theoretical and computational issues, *Phys. Rep.*, 437, 55–124, doi:10.1016/j.physrep.2006.09.005, 2006c. 1201, 1208

- Mancho, A. M., Wiggins, S., Curbelo, J., and Mendoza, C.: Lagrangian descriptors: a method for revealing phase space structures of general time dependent dynamical systems, *Commun. Nonlinear Sci.*, 18, 3530–3557, 2013. 1201, 1207
- Maxey, M. R. and Riley, J. J.: Equation of motion for a small rigid sphere in a nonuniform flow, *Phys. Fluids*, 26, 883–889, 1983. 1205
- Mendoza, C. and Mancho, A. M.: The hidden geometry of ocean flows, *Phys. Rev. Lett.*, 105, 038501, doi:10.1103/PhysRevLett.105.038501, 2010. 1201, 1207
- Mendoza, C. and Mancho, A. M.: Review Article: “The Lagrangian description of aperiodic flows: a case study of the Kuroshio Current”, *Nonlin. Processes Geophys.*, 19, 449–472, doi:10.5194/npg-19-449-2012, 2012. 1201, 1207
- Mendoza, C., Mancho, A. M., and Rio, M.-H.: The turnstile mechanism across the Kuroshio current: analysis of dynamics in altimeter velocity fields, *Nonlin. Processes Geophys.*, 17, 103–111, doi:10.5194/npg-17-103-2010, 2010. 1201
- Mendoza, C., Mancho, A. M., and Wiggins, S.: Lagrangian descriptors and the assessment of the predictive capacity of oceanic data sets, *Nonlin. Processes Geophys.*, 21, 677–689, doi:10.5194/npg-21-677-2014, 2014. 1199, 1203, 1206
- Mezic, I. and Wiggins, S.: A method for visualization of invariant sets of dynamical systems based on the ergodic partition, *Chaos*, 9, 213–218, 1999. 1201, 1202
- Mezic, I., Loire, S., Fonoberov, V. A., and Hogan, P. A.: A new mixing diagnostic and gulf oil spill movement, *Science*, 330, 486–489, 2010. 1201
- Nese, J. M.: Quantifying local predictability in phase space, *Physica D*, 35, 237–250, 1989. 1201
- Olascoaga, M. J., Beron-Vera, F., Haller, G., Trinanes, J., Iskandarani, M., Coelho, E. F., Haus, B. K., Huntley, H. S., Jacobs, G., Kirwan, A. D., Lipphardt, B. L., Ozgokmen, T. M., Reniers, A., and Valle-Levinson, A.: Drifter motion in the Gulf of Mexico constrained by altimetric Lagrangian coherent structures, *Geophys. Res. Lett.*, 40, 6171–6175, 2013. 1203
- Rempel, E. L., Chian, A. C.-L., Brandenburg, A., Munuz, P. R., and Shadden, S. C.: Coherent structures and the saturation of a nonlinear dynamo, *J. Fluid Mech.*, 729, 309–329, 2013. 1201
- Rypina, I. I., Scott, S. E., Pratt, L. J., and Brown, M. G.: Investigating the connection between complexity of isolated trajectories and Lagrangian coherent structures, *Nonlin. Processes Geophys.*, 18, 977–987, doi:10.5194/npg-18-977-2011, 2011. 1201

# Lagrangian descriptors and the surface search for MH370

V. J. García-Garrido et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion





- Saab, C.: What's our role in the search for missing flight MH370?, available at: <http://csironewsblog.com/2014/03/28/whats-our-role-in-the-search-for-missing-flight-mh370/> (last access: 20 April 2015), 2014. 1199
- Shadden, S. C., Lekien, F., and Marsden, J. E.: Definition and properties of Lagrangian coherent structures from finite-time Lyapunov exponents in two-dimensional aperiodic flows, *Physica D*, 212, 271–304, 2005. 1201, 1202
- Shadden, S. C., Lekien, F., Paduan, J. D., Chavez, F. P., and Marsden, J. E.: The correlation between surface drifters and coherent structures based on high-frequency radar data in Monterey Bay, *Deep-Sea Res. Pt. II*, 56, 161–172, 2009. 1201
- Sulman, M. H. M., Huntley, H. S., Lipphardt Jr., B. L., Jacobs, G., Hogan, P., and Kirwan Jr., A. D.: Hyperbolicity in temperature and flow fields during the formation of a Loop Current ring, *Nonlin. Processes Geophys.*, 20, 883–892, doi:10.5194/npg-20-883-2013, 2013. 1203, 1210
- Tallapragada, P. and Ross, S. D.: Particle segregation by Stokes number for small neutrally buoyant spheres in a fluid, *Phys. Rev. E*, 78, 036308, doi:10.1103/PhysRevE.78.036308, 2008. 1205
- Wiggins, S. and Mancho, A. M.: Barriers to transport in aperiodically time-dependent two-dimensional velocity fields: Nekhoroshev's theorem and “Nearly Invariant” tori, *Nonlin. Processes Geophys.*, 21, 165–185, doi:10.5194/npg-21-165-2014, 2014. 1208

## Lagrangian descriptors and the surface search for MH370

V. J. García-Garrido et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

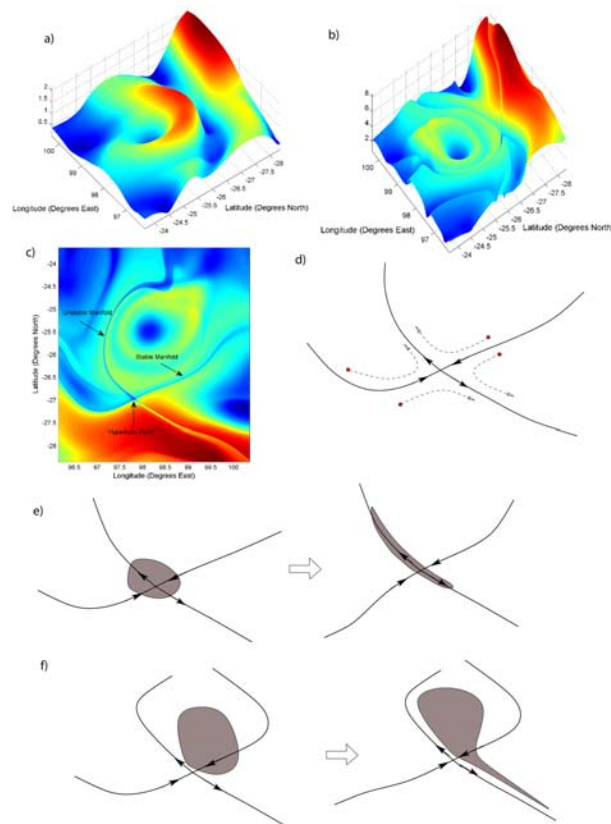
Printer-friendly Version

Interactive Discussion



# Lagrangian descriptors and the surface search for MH370

V. J. García-Garrido et al.

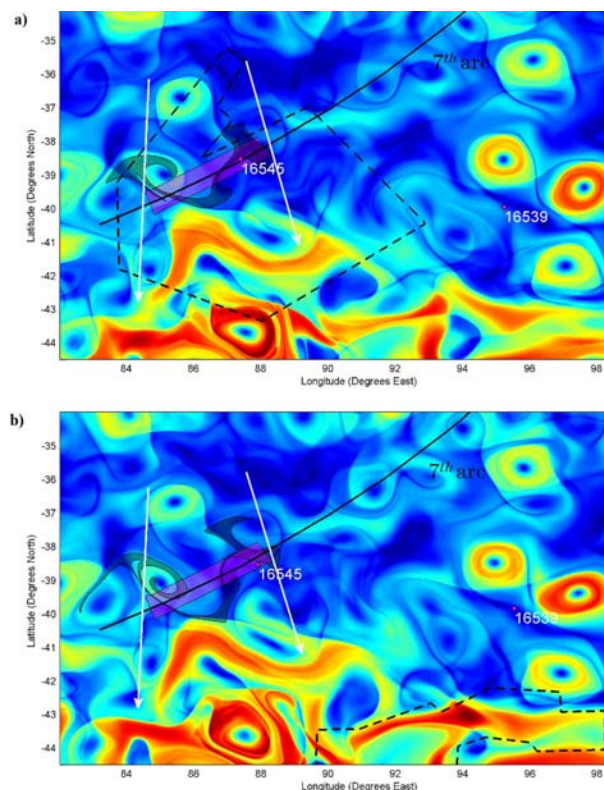


**Figure 1.** Evaluation of the  $M$  function for AVISO data in the southern Indian Ocean on the 8 March 2014. **(a)**  $\tau = 5$  days; **(b)**  $\tau = 20$  days; **(c)** a contour plot of **(b)** highlighting the position of visible invariant manifolds and a hyperbolic point; **(d)** a schematic representation of the manifolds of **(c)** showing the particle evolution in the neighborhood; **(e)** tracer blob evolution in a neighborhood of the crossing of the stable and unstable manifolds; **(f)** tracer blob evolution in a neighborhood of a hyperbolic point and an elliptic (eddy-like) region.

[Title Page](#)
[Abstract](#)
[Introduction](#)
[Conclusions](#)
[References](#)
[Tables](#)
[Figures](#)
[◀](#)
[▶](#)
[◀](#)
[▶](#)
[Back](#)
[Close](#)
[Full Screen / Esc](#)
[Printer-friendly Version](#)
[Interactive Discussion](#)


# Lagrangian descriptors and the surface search for MH370

V. J. García-Garrido et al.

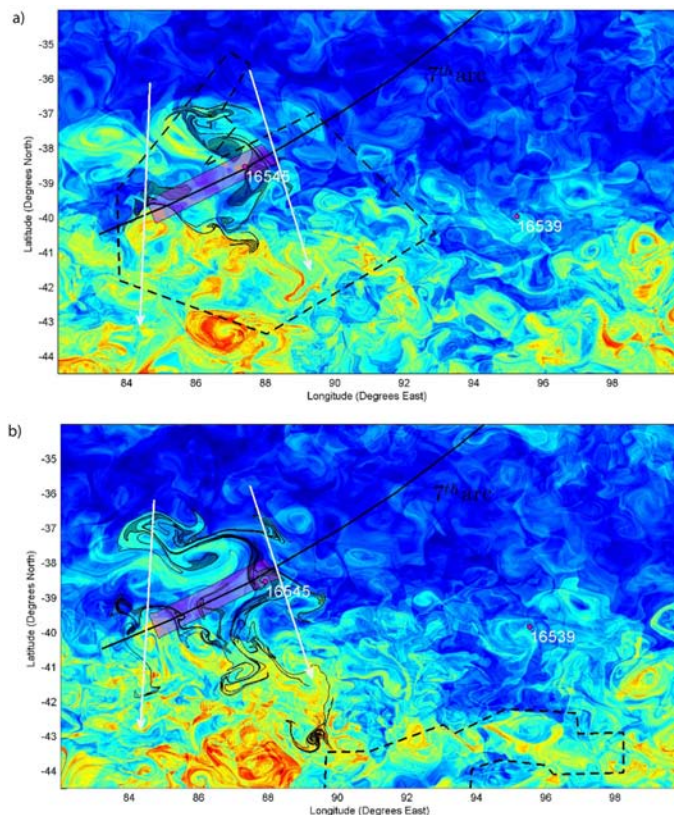


**Figure 2.** A summary of the debris search for the Malaysian MH370 plane in the southern Indian Ocean. In the background the  $M$  function, evaluated on AVISO data for  $\tau = 20$  days, highlights mesoscale structures and invariant manifolds. Overlapped are the drifters in the area (magenta dots), the expected flight paths (white arrows), the likely impact area (pink) and its contour evolution (gray). Dashed lines outline the search areas for the respective dates **(a)** 19 March 2014; **(b)** 27 March 2014.

[Title Page](#)
[Abstract](#)
[Introduction](#)
[Conclusions](#)
[References](#)
[Tables](#)
[Figures](#)
[◀](#)
[▶](#)
[◀](#)
[▶](#)
[Back](#)
[Close](#)
[Full Screen / Esc](#)
[Printer-friendly Version](#)
[Interactive Discussion](#)


# Lagrangian descriptors and the surface search for MH370

V. J. García-Garrido et al.

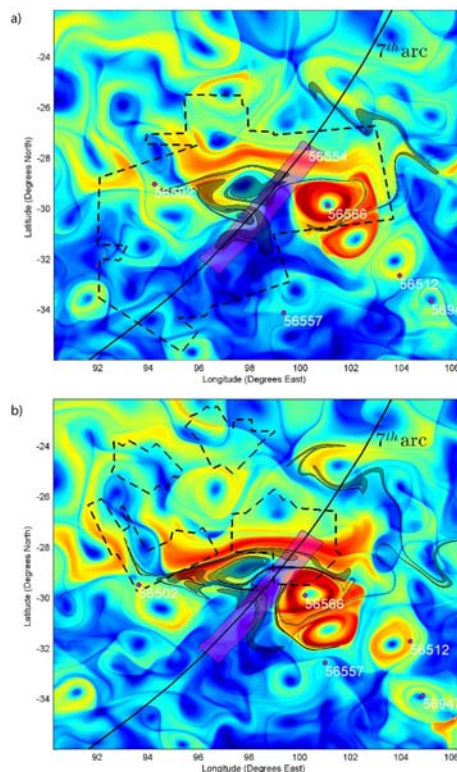


**Figure 3.** A summary of the debris search for the Malaysian MH370 plane in the southern Indian Ocean. In the background the  $M$  function, evaluated on HYCOM data for  $\tau = 15$  days at 50 m depth, highlights mesoscale structures and invariant manifolds. Overlapped are the drifters in the area (magenta dots), the expected flight paths (white arrows), the likely impact area (pink) and its contour evolution (gray). Dashed lines outline the search areas for the respective dates **(a)** 19 March 2014; **(b)** 27 March 2014.

[Title Page](#)
[Abstract](#)
[Introduction](#)
[Conclusions](#)
[References](#)
[Tables](#)
[Figures](#)
[◀](#)
[▶](#)
[◀](#)
[▶](#)
[Back](#)
[Close](#)
[Full Screen / Esc](#)
[Printer-friendly Version](#)
[Interactive Discussion](#)


# Lagrangian descriptors and the surface search for MH370

V. J. García-Garrido et al.



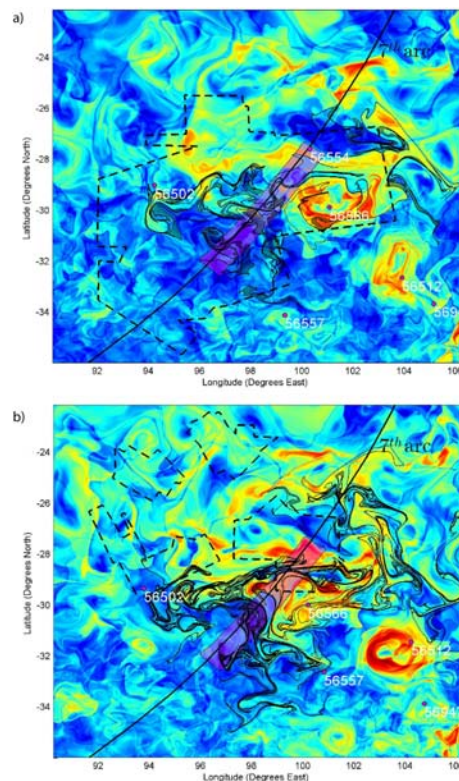
**Figure 4.** A summary of the debris search for the Malaysian MH370 plane at the north of the Broken Ridge in the Indian Ocean. In the background the  $M$  function, evaluated on AVISO data for  $\tau = 20$  days, highlights mesoscale structures and invariant manifolds. Overlapped are the drifters in the area (magenta dots), the likely impact area (pink) and its contour evolution (gray). Dashed lines surround the search areas for the respective dates **(a)** 3 April 2014; **(b)** 15 April 2014.

[Title Page](#)
[Abstract](#)
[Introduction](#)
[Conclusions](#)
[References](#)
[Tables](#)
[Figures](#)
[◀](#)
[▶](#)
[◀](#)
[▶](#)
[Back](#)
[Close](#)
[Full Screen / Esc](#)
[Printer-friendly Version](#)
[Interactive Discussion](#)




# Lagrangian descriptors and the surface search for MH370

V. J. García-Garrido et al.



**Figure 5.** A summary of the debris search for the Malaysian MH370 plane at the north of the Broken Ridge in the Indian Ocean. In the background the  $M$  function, evaluated on HYCOM data for  $\tau = 15$  days at 50 m depth, highlights mesoscale structures and invariant manifolds. Overlapped are the drifters in the area (magenta dots), the likely impact area (pink) and its contour evolution (gray). Dashed lines surround the search areas for the respective dates **(a)** 3 April 2014; **(b)** 15 April 2014.

[Title Page](#)
[Abstract](#)
[Introduction](#)
[Conclusions](#)
[References](#)
[Tables](#)
[Figures](#)
[◀](#)
[▶](#)
[◀](#)
[▶](#)
[Back](#)
[Close](#)
[Full Screen / Esc](#)
[Printer-friendly Version](#)
[Interactive Discussion](#)